

MATH 10 - TEST 1

(CHAPTER 1 and 2)

Spring 2012

NAME: Sohns

100 points

YOU MUST SHOW YOUR WORK. PRESENTATION COUNTS!

Phones must be OFF and put away. No graphing calculators allowed. No scratch paper allowed.

CIRCLE T FOR TRUE, F FOR FALSE.

(3 points each)

- T (F) (1) For any $n \times n$ matrices A , B , and C , if $AB = AC$, then $B = C$.
- T (T) F (2) If A and B are invertible $n \times n$ matrices, then AB is invertible, and $(AB)^{-1} = B^{-1} A^{-1}$.
- T (F) (3) $-3R_1 + R_2 \rightarrow R_1$ is an elementary row operation..
- T (T) F (4) The associative law for multiplication holds true for matrix multiplication.
- T (T) F (5) If A and B are square matrices such that $AB = \mathbf{0}$ and B is invertible, then $A = \mathbf{0}$.
- T (F) (6) If A is invertible then the system $AX = \mathbf{0}$ has infinitely many solutions.
- T (T) F (7) If A is row equivalent to B and A is invertible then B is invertible.
- T (F) (8) If $AB = I$ then B is the inverse of A . *must be square*

SHOW ALL WORK NEATLY AND PUT BOX AROUND ALL ANSWERS.

(9) Compute $\begin{vmatrix} 3 & -1 & 2 & 0 \\ -2 & -3 & 1 & 3 \\ 0 & -1 & 4 & 1 \\ 5 & 0 & -2 & 3 \end{vmatrix} = -170$

(8 points)

(10) a) i) $[8 \ 19 \ 21]$ ii) $B^{-1} = \begin{bmatrix} 1 & -2 & 1 \\ 0 & 1 & -1 \\ -1/3 & 0 & 2/3 \end{bmatrix}$ iii) $\begin{bmatrix} 1 & 0 & -1/3 \\ -2 & 1 & 0 \\ 1 & -1 & 2/3 \end{bmatrix}$ iv) $\frac{1}{3}$
 b) $A = \begin{bmatrix} 1 & 0 & -2 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} B$

(11) $(9, -4, 2)$

(13) Proof: Since B is $n \times m$, $B^T = m \times n$. So $B^T A B$ is $m \times m$.

$$(B^T A B)^T = B^T A^T (B^T)^T \text{ By transpose property}$$

$$= B^T A^T B \text{ " " "}$$

$$= B^T A B \text{ " " " since } A^T = A \text{ since } A \text{ symmetric.}$$

$B^T A B$ is symmetric.

(14) *Proof* $\det(A) = a^2 + b^2 + c^2 + 1 \neq 0$ for all real a, b, c so A is invertible by big thm.

- (15) If $B \neq 1$, system has a unique solution.
 If $B = 1$ and $C \neq -8$, there is no solution.
 If $B = 1$ and $C = -8$, there are infinitely many solutions.